

Precipitation Conditions

Ion Product (Q)

AKA ion quotient
* use initial concentrations



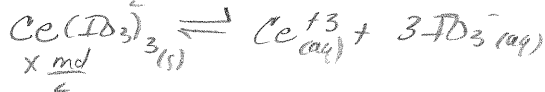
* precipitation will occur when ion product is greater than K_{sp}

If $Q > K_{sp}$ precipitation will occur ~ more solid formed

If $Q \leq K_{sp}$ no (more) precipitation occurs

Ex 1: A solution is prepared by adding 750.0 ml of $4.00 \times 10^{-3} \text{ M Ce(NO}_3)_3$ to 300.0 ml of $2.00 \times 10^{-2} \text{ M KIO}_3$. Will $\text{Ce(IO}_3)_3$ ($K_{sp} = 1.9 \times 10^{-10}$) precipitate from this solution?

(0.300L) (2.00 x 10^-2 mol/L) = 6.00 x 10^-3 mol IO3-



$$(0.750\text{L})(4.00 \times 10^{-3} \text{ mol/L}) = 3.00 \times 10^{-3} \text{ mol Ce}^{3+}$$

$$K_{sp} = [\text{Ce}^{3+}][\text{IO}_3^{-}]^3$$

$$\begin{aligned} Q &= [\text{Ce}^{3+}]_0 [\text{IO}_3^{-}]_0^3 \\ &= (2.86 \times 10^{-3} \text{ M})(5.71 \times 10^{-3} \text{ M})^3 \\ &= 5.32 \times 10^{-10} \end{aligned}$$

$$[\text{Ce}^{3+}] = \frac{3.00 \times 10^{-3} \text{ mol}}{1.05 \text{ L}} = 2.86 \times 10^{-3} \text{ M Ce}^{3+}$$

$$[\text{IO}_3^{-}] = \frac{6.00 \times 10^{-3} \text{ mol}}{1.05 \text{ L}} = 5.71 \times 10^{-3} \text{ M IO}_3^{-}$$

$Q > K_{sp} \therefore$ precipitation will occur



SELECTIVE PRECIPITATION

→ "separating ions by precipitation"

*Selective Precipitation is often utilized to separate ions present in solution.

Ex: A solution of Ag^+ , NO_3^- and Ba^{+2} ions

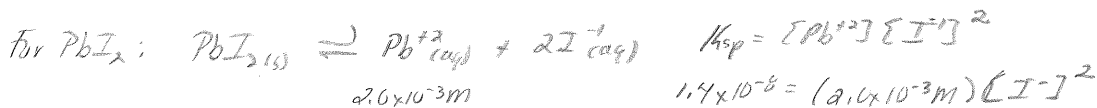
NaCl is added to solution → $\text{Na}^+ \sim$ soluble w/ NO_3^-
 $\text{Cl}^- \rightarrow \text{AgCl}$ insoluble

Na_2SO_4 is added to original solution → $\text{Na}^+ \sim$ soluble w/ NO_3^-
 $\text{SO}_4^{2-} \rightarrow \text{BaSO}_4$ insoluble

**Ions are separated by precipitation. **

**Metal sulfides vary greatly in their solubility, therefore sulfide ion is often utilized in selective precipitation.

Ex: A solution contains $1.0 \times 10^{-4} \text{ M Cu}^+$ and $2.0 \times 10^{-3} \text{ M Pb}^{+2}$. If a source of I^- is gradually added to this solution, will PbI_2 ($K_{\text{sp}} = 1.4 \times 10^{-8}$) or CuI ($K_{\text{sp}} = 5.3 \times 10^{-12}$) precipitate first? Specify the concentration of I^- necessary to begin precipitation of each salt.



$$2.6 \times 10^{-3} \text{ M} = [\text{I}^-]$$

* any I^- in excess of $2.6 \times 10^{-3} \text{ M}$ will cause $\text{PbI}_2(s)$ to form



$$K_{\text{sp}} = [\text{Cu}^+][\text{I}^-]$$

$$5.3 \times 10^{-12} = (1.0 \times 10^{-4} \text{ M})[\text{I}^-]$$

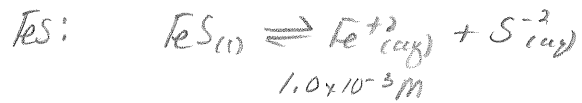
$$5.3 \times 10^{-8} \text{ M} = [\text{I}^-]$$

* any I^- in excess of $5.3 \times 10^{-8} \text{ M}$ will cause $\text{CuI}(s)$ to form

$\text{CuI}(s)$ will precipitate first
 (requires less I^-)

∴ Cu^+ would be separated by Pb^{+2} when $[\text{I}^-] > 5.3 \times 10^{-8} \text{ M}$

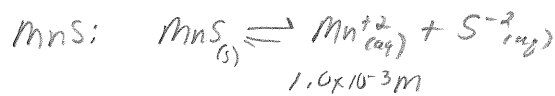
Ex: A solution contains $1.0 \times 10^{-3} \text{ M Fe(NO}_3)_2$ and $1.0 \times 10^{-3} \text{ M MnSO}_4$. Both Fe^{+2} and Mn^{+2} form sulfide salts: FeS ($K_{\text{sp}} = 3.7 \times 10^{-19}$) and MnS ($K_{\text{sp}} = 1.4 \times 10^{-15}$). If sulfide ion is added to the solution containing $10^{-3} \text{ M Fe}^{+2}$ and $10^{-3} \text{ M Mn}^{+2}$, which sulfide salt will precipitate first and at what $[\text{S}^{2-}]$ will precipitation occur?



$$K_{\text{sp}} = [\text{Fe}^{+2}][\text{S}^{2-}] = 3.7 \times 10^{-19}$$

$$(1.0 \times 10^{-3} \text{ M})[\text{S}^{2-}] = 3.7 \times 10^{-19}$$

$$[\text{S}^{2-}] = 3.7 \times 10^{-16} \text{ M}$$



$$K_{\text{sp}} = [\text{Mn}^{+2}][\text{S}^{2-}] = 1.4 \times 10^{-15}$$

$$(1.0 \times 10^{-3} \text{ M})(\text{S}^{2-}) = 1.4 \times 10^{-15}$$

$$[\text{S}^{2-}] = 1.4 \times 10^{-12} \text{ M}$$

$\therefore \text{FeS}$ will precip. first
when $[\text{S}^{2-}] > 3.7 \times 10^{-16} \text{ M}$

